THE OPTIMIST CLASSES
IIT-JAM TOPPERS

8 AIR — MANOJ KUMAR SINGH

9 AIR — ABHAY

12 AIR — PAWAN

15 AIR — SATYAM

21 AIR — SOUMIL GIRISH SAHU

29 AIR — BHOOMIJA

31 AIR — AKSHIT AGGARWAL

32 AIR — SHIKHAR CHAMOLI

33 AIR — RAVI SINGH ADHIKARI

44 AIR — GAURAV JHA

56 AIR — SWAPNIL JOSHI

65 AIR — LOKESH BHATT

75 AIR — GOPESH VISHVAKARMA

77 AIR — VAIBHAV

80 AIR — SHASWAT CHAMOLI

CSIR-NET-JRF RESULTS 2022

102 AIR — JRF
ANNU
DL01000308

133 AIR — JRF
ALANKAR
UP15000162

155 AIR — JRF
SAHIL RANA
HR09000108

168 AIR — JRF
JAYESTHI
RJ11000161

174 AIR — JRF
DASRATH
RJ06000682

181 AIR — JRF
VIVEK
UK01000439

183 AIR — JRF
UZAIR AHMED
UP02000246

191 AIR — JRF
SURYA PRATAP SINGH
RJ06000232

195 AIR — JRF
HIMANSHU
UP10000095

222 AIR — JRF
CHANDAN
RJ09000159

228 AIR — JRF
SAIKHOM JOHNSON
MN01000196

231 AIR — JRF
AJAY SAINI
RJ06001744

258 AIR — JRF
VIKAS YADAV
RJ06001102
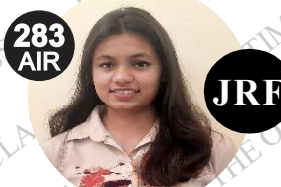
283 AIR — JRF
JYOTSNA KOHLI
UK02000262

318 AIR — JRF
SHYAM SUNDAR
RJ06000615

THE OPTIMIST CLASSES

AN INSTITUTE FOR NET-JRF/GATE/IIT-JAM/JEST/TIFR/M.Sc ENTRANCE EXAMS

CONTACT: 9871044043

IIT - JAM PHYSICS

## PREVIOUS YEAR QUESTION 2014

Q. 1 - Q. 10 carry one mark each.

1. For vectors $\vec{a} = \hat{j} + \hat{k}, \vec{b} = 2\hat{i} + 3\hat{j} - 5\hat{k}$ and $\vec{c} = \hat{j} - \hat{k}$, the vector product $\vec{a} \times (\vec{b} \times \vec{c})$ is

   (a) in the same direction as $\vec{c}$

   (b) in the dirction opposite to $\vec{c}$

   (c) in the same direction as $\vec{b}$

   (d) in the direction opposite to $\vec{b}$

2. A particle of mass m carrying charge q is moving in a circle in a magnetic field B. According to Bohr's model, the energy of the particle in the nth level is

   (a) $\frac{1}{n^2}\left(\frac{hqB}{\pi m}\right)$ 　　(b) $n\left(\frac{hqB}{\pi m}\right)$ 　　(c) $n\left(\frac{hqB}{2\pi m}\right)$ 　　(d) $n\left(\frac{hqB}{4\pi m}\right)$

3. A conducting slab of copper PQRS is kept on the xy plane in a uniform magnetic field along x-axis as indicated in the figure. A steady current I flows through the cross section of the slab along the y-axis. The direction of the electric field inside the slab, arising due to the applied magnetic field is along the
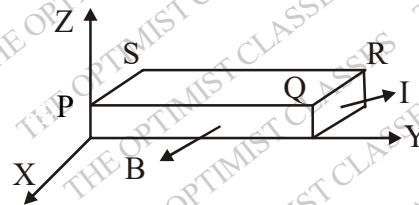

   (a) negative Y direction 　　　　　　　(b) positive Y direction

   (c) negative Z direction 　　　　　　　(d) positive Z direction

4. A collimated beam of light of diameter 1 mm is propagating along the x-axis. The beam is to be expanded to a collimated beam of diameter 10 mm using a combination of two convex lenses. A lens of focal length of 50 mm and another lens with focal length F are to be kept at a distance d between them. The values of F and d respectively, are

   (a) 450 mm and 10 mm 　　　　　　　(b) 400 mm and 500 mm

   (c) 550 mm and 600 mm 　　　　　　　(d) 500 mm and 550 mm

5. Octal equivalent of decimal number 478_{10} is

   (a) 736_8 　　　　(b) 673_8 　　　　(c) 637_8 　　　　(d) 367_8

6. A spherical ball of ice has radius R_0 and is rotating with an angular speed ω about an axis passing through its centre. At time t = 0, it starts acquiring mass because the moisture (at rest) around it starts to freeze on it uniformly. As a result its radius increases as $R(t) = R_0 + \alpha t$, where α is a constant. The curve which best

describes its angular speed with time is

(a) (b) (c) (d)
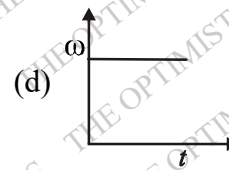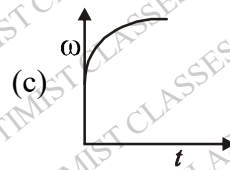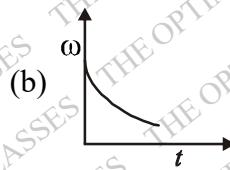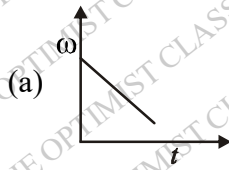
7. In 1-dimension, an ensemble of N classical particle has energy of the form $E = \dfrac{p_x^2}{2m} + \dfrac{1}{2}kx^2$. The average internal energy of the system at temperature T is

(a) $\dfrac{3}{2}Nk_BT$ (b) $\dfrac{1}{2}Nk_BT$ (c) $3Nk_BT$ (d) Nk_BT

8. In a photoelectric effect experiment, ultraviolet light of wavelength 320 nm falls on the photocathode with work function of 2.1 eV. The stopping potential should be close to
(a) 1.8 V (b) 1.6 V (c) 2.2 V (d) 2.4 V

9. In an ideal operational amplifier depicted below, the potential at node A is
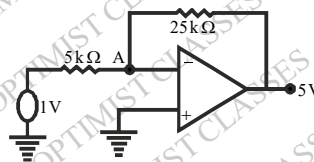

(a) 1 V (b) 0 V (c) 5 V (d) 25 V

10. To operate a npn transistor in active region, its emitter-base and collector-base junction respectively, should be
(a) forward biased and reversed biased (b) forward biased and forward biased
(c) reversed biased and forward biased (d) reversed biased and reversed biased

Q. 11 - Q. 35 carry two marks each.

11. The value of $\displaystyle\sum_{n=0}^{\infty} r^n \sin(n\theta)$ for $r = 0.5$ and $\theta = \dfrac{\pi}{3}$ is

(a) $\dfrac{1}{\sqrt{3}}$ (b) $\sqrt{\dfrac{2}{3}}$ (c) $\sqrt{\dfrac{3}{2}}$ (d) $\sqrt{3}$

12. In a parallel plate capacitor the distance between the plates is 10 cm. Two dielectric slabs of thickness 5cm each and dielectric constants $K_1 = 2$ and $K_2 = 4$ respectively, are inserted between the plates. A potential of 100V is applied across the capacitor as shown in the figure. The value of the net bound surface charge density at the interface of the two dielectric is
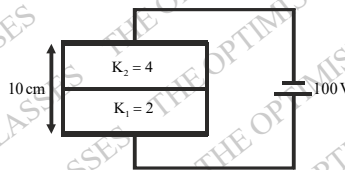
(a) $-\dfrac{2000}{3}\varepsilon_0$ (b) $-\dfrac{1000}{3}\varepsilon_0$ (c) $-250\varepsilon_0$ (d) $\dfrac{2000}{3}\varepsilon_0$

13. The electric fields of two light sources with nearby frequencies ω_1 and ω_2, and wave vector k_1 and k_2, are expressed as $\vec{E}_1 = E_{10}\hat{i}e^{-i(k_1 z - \omega_1 t)}$ and $\vec{E}_2 = E_{20}\hat{i}e^{-i(k_2 z - \omega_2 t)}$, respectively. The interference pattern on the screen is photographed at $t = t_0$; denote $(k_1 - k_2)z - (\omega_1 - \omega_2)t_0$ by θ. For this pattern

(a) a bright fringe will be obtained for $\cos\theta = -1$

(b) a bright fringe intensity is given by $\left(E_{10}\right)^2 + \left(E_{20}\right)^2$

(c) a dark fringe will be obtained for $\cos\theta = 1$

(d) a dark fringe intensity is given by $\left(E_{10} - E_{20}\right)^2$

14. A solid metallic cube of heat capacity S is at temperature $300K$. It is brought in contact with a reservoir at $600K$. If the heat transfer takes place only between the reservoir and the cube, the entropy change of the universe after reaching the thermal equilibrium is

(a) $0.69\,S$ (b) $0.54\,S$ (c) $0.27\,S$ (d) $0.19\,S$

15. If the surface integral of the field $\vec{A}(x,y,z) = 2\alpha x\hat{i} + \beta y\hat{j} - 3\gamma z\hat{k}$ over the closed surface of an arbitrary unit sphere is to be zero, then the relationship between α, β and γ is

(a) $\alpha + \beta/6 - \gamma = 0$ (b) $\alpha/3 + \beta/6 - \gamma/2 = 0$

(d) $\alpha/2 + \beta - \gamma/3 = 0$ (d) $2/\alpha + 1/\beta - 3/\gamma = 0$

16. The moment of inertia of a disc about one of its diameters is I_M. The mass per unit area of the disc is proportional to the distance from its centre. If the radius of the disc is R and its mass is M, the value of I_M is

(a) $\frac{1}{2}MR^2$ (b) $\frac{2}{5}MR^2$ (c) $\frac{3}{10}MR^2$ (d) $\frac{3}{5}MR^2$

17. A rigid uniform horizontal wire PQ of mass M, pivoted at P, carries a constant current I. It rotates with a constant angular speed in a uniform vertical magnetic field B. If the current were switched off, the angular acceleration of the wire, in terms of B, M and I would be
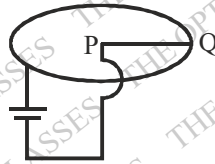
(a) 0 (b) $\frac{2BI}{3M}$ (c) $\frac{3BI}{2M}$ (d) $\frac{BI}{M}$

18. Two points N and S are located in the northern and southern hemisphere, respectively, on the same longitude. Projectiles P and Q are fired from N and S, respectively, towards each other. Which of the following options is correct for the projectiles as they approach the equator?

(a) Both P and Q will move towards the east

(b) Both P and Q will move towards the west

(c) P will move towards the east and Q towards the west

(d) P will move towards the west and Q towards the east

19. Two particles A and B of mass m and one particle C of mass M are kept on the x-axis in the order ABC.

Particle A is given a velocity $v\hat{i}$. Consequently there are two collisions, both of which are completely inelastic. If the net energy loss because of these collisions is 7/8 of the initial energy, the value of M is (ignore frictional losses)

(a) $8\,m$ (b) $6\,m$ (c) $4\,m$ (d) $2\,m$

20. The line integral $\oint \vec{A}.d\vec{l}$ of a vector field $\vec{A}(x,y) = \frac{1}{r^2}\left(-y\hat{i} + x\hat{j}\right)$, where $r^2 = x^2 + y^2$, is taken around a square (see figure) of side unit length and centered at (x_0, y_0) with $|x_0| > \frac{1}{2}$ and $|y_0| > \frac{1}{2}$. If the value of the integral is L, then
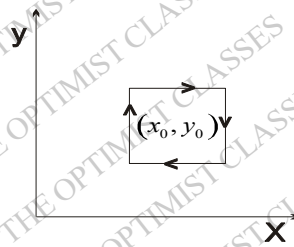
(a) L depends on (x_0, y_0)

(b) L is independent of (x_0, y_0) and its value is -1

(c) L is independent of (x_0, y_0) and its value of 0

(d) L is independent of (x_0, y_0) and its value is 2

21. Diamond lattice can be considered as a combination of two fcc lattices displaced along the body diagonal by one quarter of its length. There are eight atoms per unit cell. The packing fraction of the diamond structure is
    (a) 0.48   (b) 0.74   (c) 0.34   (d) 0.68

22. Thermal neutrons (energy $= 300k_B = 0.025\,eV$) are sometimes used for structural determination of materials. The typical lattice spacing of a material for which these can be used is
    (a) $0.01\ nm$ (b) $0.05\ nm$ (c) $0.1\ nm$ (d) $0.15\ nm$

23. What is the maximum height above the dashed line attained by the water stream coming out at B from a thin tube of the water tank assembly shown in the figure? Assume $h = 10\,\text{m}$, $l = 2\text{m}$, and $\theta = 30°$.
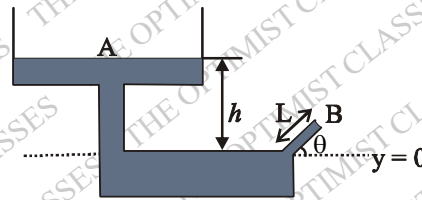
    (a) $10\ m$ (b) $2\ m$ (c) $1.2\ m$ (d) $3.2\ m$

24. A steady current in a straight conducting wire produces a surface charge on it. Let E_{out} and E_{in} be the magnitude of the electric fields just outside and just inside the wire, respectively. Which of the following statements is true for these fields?

(a) E_{out} is always greater than E_{in}

(b) E_{out} is always smaller than E_{in}

(c) E_{out} could be greater or smaller than E_{in}

(d) E_{out} is equal to E_{in}

25. A small charged spherical shell of radius $0.01\ m$ is at a potential of $30V$. The electrostatic energy of the shell is
    (a) 10^{-10} J   (b) 5×10^{-10} J   (c) 5×10^{-9} J   (d) 10^{-9} J

26. At an instant shown three point masses m, $2m$ and $3m$ rest on a horizontal surface, and are at the vertices of an equilateral triangle of unit side length. Assuming that G is the gravitational constant, the magnitude and direction of the torque on the mass $3m$, about the point O, at that instant is
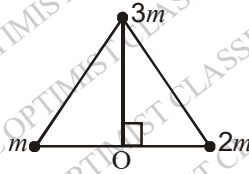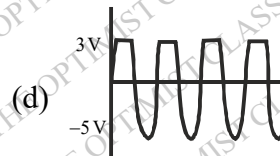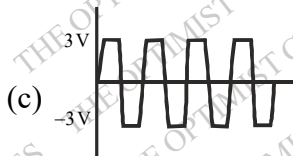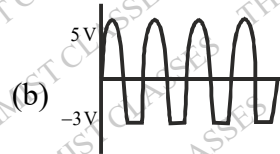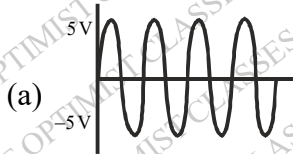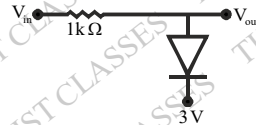
(a) zero

(b) $\frac{3}{2}G\sqrt{3}m^2$, going into the paper

(c) $3G\sqrt{3}m^2$, coming out of th paper

(d) $\frac{3}{4}G\sqrt{3}m^2$, going into the paper

27. A sine wave of $5V$ amplitude is applied at the input of the circuit shown in the figure. Which of the following waveforms represents the output most closely?

(a)

(b)

(c)

(d)

28. 1011 binary input have been applied at X_3, X_2, X_1, X_0 input in the shown logic circuit made of *XOR* gates. The binary output Y_3, Y_2, Y_1, Y_0 of the circuit will be
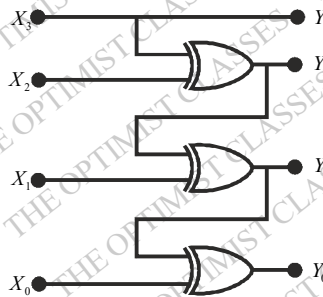
(a) 1101   (b) 1010   (c) 1111   (d) 0101

29. A ring of radius R carries a linear charge density λ. It is rotating with angular speed ω. The magnetic field at its centre is

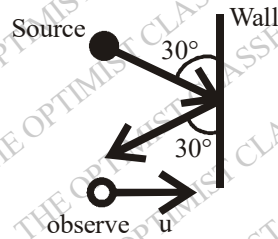(a) $\frac{3\mu_0\lambda\omega}{2}$ (b) $\frac{\mu_0\lambda\omega}{2}$ (c) $\frac{\mu_0\lambda\omega}{\pi}$ (d) $\mu_0\lambda\omega$

30. A stationary source (see figure below) emits sound waves of frequency f towards a wall. If an observer moving with speed u in a direction perpendicular to the wall, measures a frequency $f' = \frac{9}{8}f$ at the instant shown, then u is related to the speed of sound V_s as

(a) V_s (b) $V_s/2$ (c) $V_s/4$ (d) $V_s/8$

31. A real gas has specific volume v at temperature T. Its coefficient of volume expansion and isothermal compressibility are α and k_T, respectively. Its molar specific heat at constant pressure C_p and molar specific heat at constant volume C_v are related as

(a) $C_p = C_v + R$ (b) $C_p = C_v + \dfrac{Tv\alpha}{k_T}$ (c) $C_p = C_v + \dfrac{Tv\alpha^2}{k_T}$ (d) $C_p = C_v$

32. Two frames, O and O', are in relative motion as shown. O' is moving with speed $c/2$, where c is the speed of light. In frame O, two separate events occure at (x_1, t_1) and (x_2, t_2). Inf frame O', these events occur simultaneously. The value of $(x_2 - x_1)/(t_2 - t_1)$ is

(a) $c/4$ (b) $c/2$ (c) $2c$ (d) c

33. White light is incident on a grating G_1 with groove density 600 lines/nm and width 50mm. A small portion of the diffracted light is incident on another grating G_2 with groove density 1800 lines/mm and width 15mm. The resolving power of the combined system is

(a) 3×10^3 (b) 57×10^3 (c) 81×10^7 (d) 108×10^5

34. Four particles of mass m each are inside a two dimensional square box of side L. If each state obtained from the solution of the Schrodinger equation is occupied by only one particle, the minimum energy of the system in units of $\dfrac{h^2}{mL^2}$ is

(a) 2   (b) $\dfrac{5}{2}$ (c) $\dfrac{11}{2}$ (d) $\dfrac{25}{4}$

35. At atmospheric pressure $(= 10^5 \text{ Pa})$, aluminium melts at 550K. As it melts, its density decreases from $3 \times 10^3 \text{ kg/m}^3$ to $2.9 \times 10^3 \text{ kg/m}^3$. Latent heat of fusion of aluminium is $24 \times 10^3 \text{ J/kg}$. The melting point of aluminium at a pressure of 10^7 Pa is closest to

(a) 551.3 K   (b) 552.6 K   (c) 558.7 K   (d) 547.4 K

**Q. 36 - Q. 43 carry five marks each.**

36. Find the solution of the differential equation $\dfrac{d^2y}{dx^2} + 5\dfrac{dy}{dx} = 0$ with the boundary condition $y(0) = 2$ and $\left. \dfrac{dy}{dx} \right|_{x=0} = 2$, giving all steps clearly. Find the value of x where $y = 0$.

37. The electric field in an electromagnetic (*EM*) wave is $\vec{E} = \sqrt{6\pi}\,\hat{i}\sin[2\pi(10^6 z - 3\times10^{14}t)]$. What is the intensity of the *EM* wave and the number of photons per second falling on the unit area of a perfectly reflecting screen kept perpendicular to the direction of propagation? When a photon in this beam is reflected from the screen, what is the impulse it imparts to the screen? Use this to find the pressure exerted by the EM wave on the screen.

38. A unifrom rod of mass m and length l is hinged at one of its ends O and is hanging vertically. It is hit at its midpoint with a very short duration impulse J so that it starts rotating about O. Find the magnitude and direction of the horizontal impulse that O applies on the rod when it is hit.

39. **An easy derivation of $\mathrm{PV}^{\gamma} = $ constant for an ideal gas undergoing an adiabatic process:**
Consider P and V as the basic variables of an ideal gas and write the heat exchanged dQ in terms of dV and dP. Next, using the definition of C_P and C_V in the expression for dQ, obtain a differential equation relating P and V for an adiabatic process and solve it to get the desired relationship. Derivation SHOULD NOT use the first law of thermodynamics. [For a function $f(x, y)$ the differential $df = \left(\dfrac{\partial f}{\partial x}\right)_y dx + \left(\dfrac{\partial f}{\partial y}\right)_x dy$]

40. As shown in the figure below, an unpolarised beam of light of wavelength 500nm is incident on a linear polariser at AF with vertical polarisation. The light beam then passes through a wave plate BE (half wave or quarter wave plate) of thickness 1.00125 mm and gets reflected from a mirror CD. The reflected light if indicated by the dashed line (DEF) in the diagram. The ordinary and extraordinary refractive indices for the mterial of the wave plate are 1.658 and 1.558, respectively. Light is incident normally on all surface.
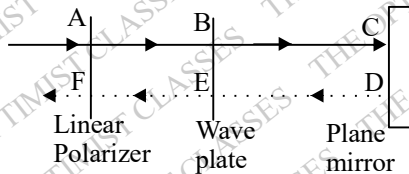
(a) What is the polarisation of the beam at C?
(b) What is the polarisation of the beam at E and F?

41. A standing wave of light is formed between two mirrors and a beam of atoms is incident on it normally (see figure below) from the left. On the right side, atoms are detected in the direction of the beam and also at an angle θ as shown in the figure. This is due to material waves of atoms diffracted by the standing wave that acts like a grating the slit width of tis grating is given by the distance between two maxima of the light intensity. If the atomic beam is made of atoms of mass m moving with speed v and the light wave has wavelength λ_L, find the smallest angle θ by using the diffraction condition.

Atomic beam
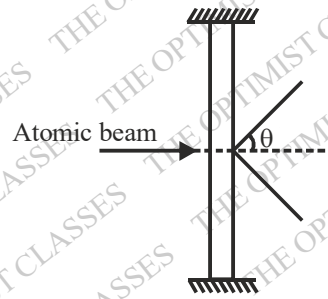
42. According to Wien's theory of black body radiation, the spectral energy density in a blackbody cavity at temperature T is given as

$$u_T(\lambda)d\lambda = \frac{\alpha}{c^3\lambda^5}e^{-\beta/\lambda T}d\lambda$$

where α and β are constants and c is the speed of light. Further, the intensity of radiation coming out of the

cavity is $\frac{u_T c}{4}$, where $u_T = \int_0^\infty u_T(\lambda)d\lambda$ is the total energy density of radiation. Given that Stefan-Boltzmann

constant $\sigma = 5.67\times10^{-8}$ Wm^{-2}K^{-4} and $\lambda_{max}T = 2.90\times10^{-3}$ m.K , find the values of α and β. The value of

integral $\int_0^\infty x^3 e^{-x}dx = 6$.

43. A horizontal rod of proper length L moves with uniform speed V > 0 along the x-axis of a coordinate frame. A ground observer measures the position coordinates of its two ends at two different times, with time difference $\Delta t > 0$. The observer finds that the difference between the two coordinates is L. Calculate Δt in terms of L, V and the speed of light c. If measured correctly, what would have been the length of the rod in the ground frame?

ANSWER KEY

1.	(a)	2.	(d)	3.	(c)	4.	(d)	5.	(a)	6.	(b)	7.	(d)
8.	(a)	9.	(b)	10.	(b)	11.	(a)	12.	(a)	13.	(d)	14.	(d)
15.	(*)	16.	(c)	17.	(c)	18.	(b)	19.	(b)	20.	(c)	21.	(c)
22.	(c)	23.	(d)	24.	(b)	25.	(b)	26.	(d)	27.	(d)	28.	(a)
29.	(b)	30.	(c)	31.	(c)	32.	(c)	33.	(c)	34.	(b)	35.	(b)
36.	(*)	37.	(*)	38.	(*)	39.	(*)	40.	(*)	41.	(*)	42.	(*)
43.	(*)												